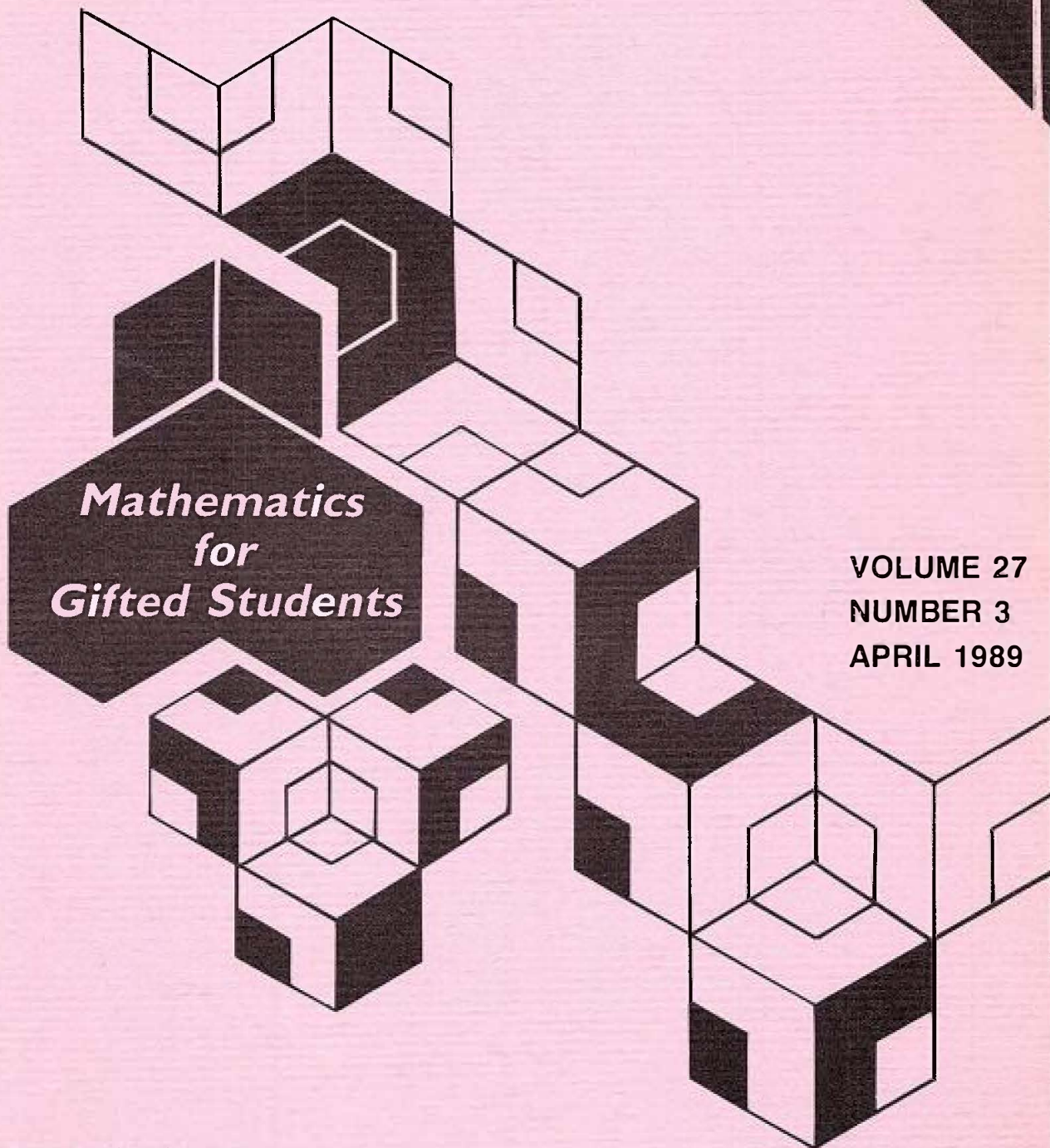


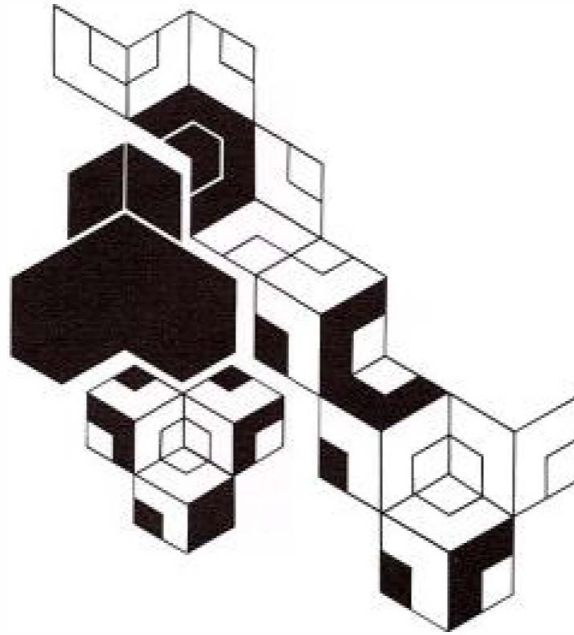
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Mathematics for Gifted Students

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Guest Editor, Andy Liu

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Kathy Jones, a Hungarian-born inventor, is the president and chief executive officer of Kadon Enterprises, Inc., a company which produces top quality mathematical games and puzzles. Her background is in philosophy and commercial arts. Before venturing into her own business, she was a ballroom dance instructor and competition dancer. She is a member of the Imperial Society (London) of Teachers of Dancing. She regards artistic expression, whether through dance movement or mathematical symmetry, as a way of creating order and harmony amid the apparent chaos and discord of the world. Her game and puzzle designs are a celebration of the mind's ability to see beauty in the systems and structures of both nature and the mind's own creations. She is the inventor of "Lemma," a logical system-building game and the developer of many combinatorial puzzle sets.

Tony Gardiner combines research in combinatorics and group theory with a wider interest in mathematics, in its history and in how human beings—young and old—make the subject their own. His three books, *Infinite Processes* (Springer), *Discovering Mathematics* (Oxford) and *Mathematical Puzzling* (Oxford), reflect this breadth of interest. He has worked with many groups of interested youngsters and is currently establishing a national mathematics competition which is aimed at 30 percent of the fourteen-year-olds in the United Kingdom.

Mogens Esrom Larsen was born in 1942, graduated from the University of Copenhagen in 1965 and has been an associate professor of the department of mathematics there since, except for one year, 1969-70, when he visited the Massachusetts Institute of Technology. His interests cover most of mathematics, including functions of several complex variables, differential equations, finite groups and Rubik's cubes, pre-Euclidean history of mathematics, numerical analysis and the teaching and applications of modern mathematics. He writes a monthly problem column on popular science, where pentominoes frequently appear, for a Scandinavian journal. A game enthusiast, he was the founder of the Copenhagen Go Club in 1972.

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