

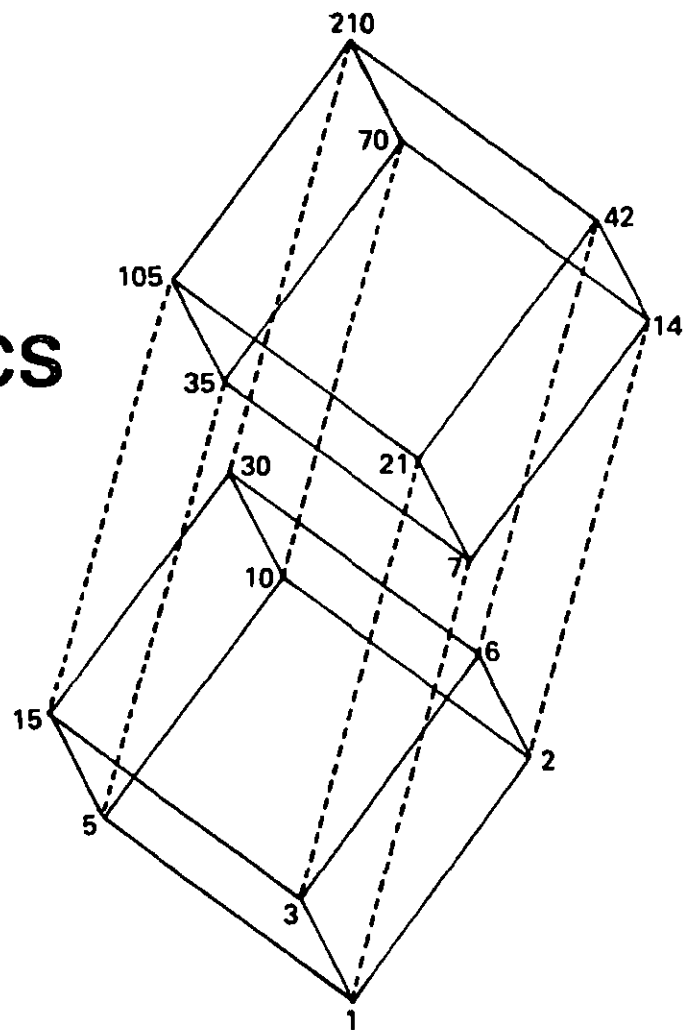
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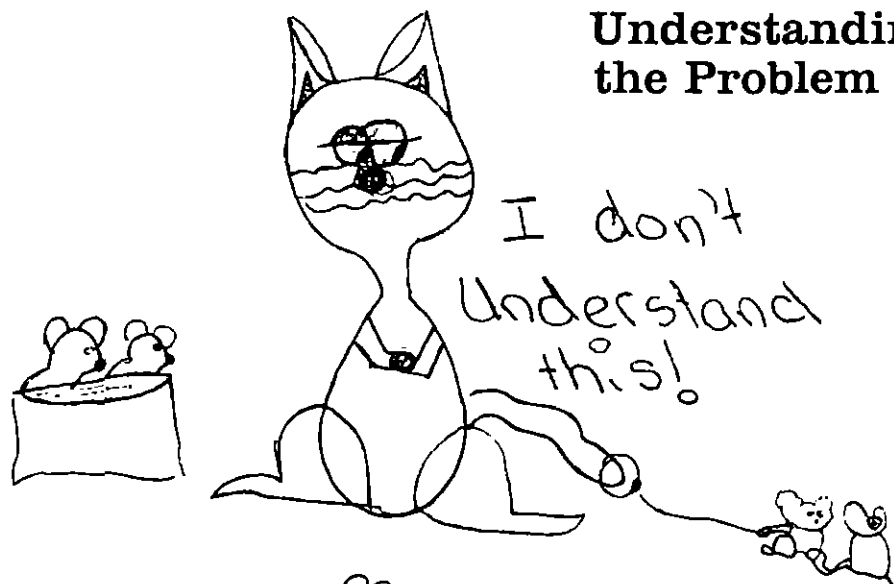
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Problem Solving in the Mathematics Classroom



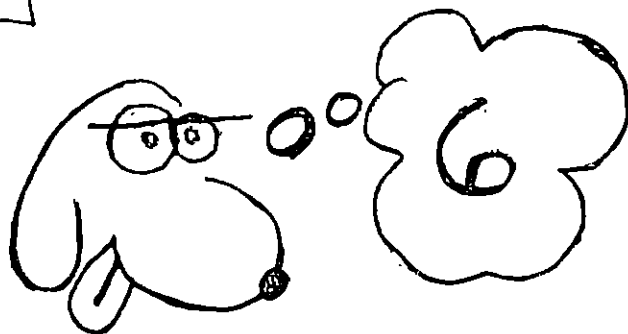
Problem-Solving Strategies

Understanding the Problem



Devising a Plan

Elisa
Hollenberg



Should I start guessing, and if so where?

Cindy
McLeod
U.S.

MATH Monograph No. 7



April 1982

Problem Solving in the Mathematics Classroom

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